# Vibrational Raman Optical Activity in <br> $(R)-(+)-3-M e t h y l c y c l o h e x a n o n e: ~ E x p e r i m e n t a l ~ a n d ~ a b ~ I n i t i o ~$ <br> Theoretical Studies and the Origins of the Unusual Couplets 

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#### Abstract

Vibrational Raman optical activity (ROA) spectra of 3-methylcyclohexanone with excellent signal-to-noise ratio obtained on a new ROA spectrometer and corresponding ab initio theoretical ROA spectra obtained with $6-31 \mathrm{G}$ and $6-31 \mathrm{G}^{*}$ basis sets are presented. The experimental ROA spectrum for the ( + )-enantiomer compares well with the predicted ROA spectra for the ( $R$ )-configuration of 3 -methylcyclohexanone. This allows us to confidently suggest the origins of several bisignate couplets present in the experimental spectrum which had previously attracted much speculative discussion.


## Introduction

The potential of vibrational Raman optical activity (ROA) for three-dimensional molecular structure determination is being established rapidly. Although the ROA phenomenon was predicted ${ }^{1}$ and observed ${ }^{2}$ in the early 1970s, the progress in establishing ROA as a practical spectroscopic tool has been hampered by low instrumental sensitivity and lack of reliable theoretical models. Only a few years ago, the experimental measurements still appeared too difficult and successful theoretical predictions were thought to be out of reach. Recent developments both in theoretical methods and experimental techniques, however, have changed this situation. It was recognized ${ }^{3,4}$ that ROA can be predicted from first principles, and the subsequent implementation of an $a b$ initio algorithm has now made it possible to interpret experimental ROA spectra ${ }^{5-13}$ with more confidence. At about the same time, introduction of charge coupled device (CCD) detectors into ROA spectroscopy has greatly improved the quality of ROA spectra. ${ }^{14.15}$ It was also realized that the ROA artifacts are minimized in backscattering and that this geometry is necessary for studies on biological samples. ${ }^{15,16}$ Different polarization modulation schemes for ROA measure-

[^0]ments have also been formulated and implemented. ${ }^{17-21}$ As a result of these simultaneous advances in experimental techniques and theoretical methods, ROA spectroscopy is becoming a practical tool for determining three-dimensional chiral molecular structures in the solution phase.

Methylcyclohexanone is one of the molecules that has attracted much attention for vibrational optical activity (VOA) studies in the last decade. ${ }^{22-29}$ In the early stages of VOA research, empirical methods were tested on small molecules to verify the validity of those methods by comparing experimental observations with theoretical predictions. For theoretical predictions a knowledge of appropriate force fields with reliable force constants for the molecule under study is essential. The availability of empirical force constants for cyclohexanone ${ }^{30}$ facilitated the situation for methylcyclohexanone because the concept of transferability of force constants appeared reasonable in these cases. Different vibrational circular dichroism (VCD) ${ }^{22-24}$ and $\mathrm{ROA}^{23.26-29}$ analyses were reported for 3 -methylcyclohexanone. In all these studies, the vibrational assignments were derived empirically and could not be verified through an independent method. The $a b$ initio quantum theoretical methods are the most reliable approaches currently available for both vibrational normal mode compositions as well as ROA predictions and therefore provide a better understanding of ROA in 3-methylcyclohexanone than the previous empirical methods. We are not aware of any prior $a b$ initio vibrational studies for this molecule.
The absolute configuration and predominant conformation of $(+)-3$-methylcyclohexanone have been known for a long time. The ( + )-enantiomer of 3 -methylcyclohexanone has the ( $R$ )configuration, and the chair conformation with the methyl group in an equatorial position is energetically favored over that with

[^1]

Figure 1. Experimental depolarized Raman and ROA spectra for $(R)$ -$(+)$-3-methylcyclohexanone.
an axial methyl group and the twisted ring conformers. ${ }^{31}$ There is no apparent need to reinvestigate the absolute configuration and conformations of methylcyclohexanone, but verifications of the ROA predictions for known structures are necessary for validating the ab initio theoretical model ${ }^{3,4}$ that is in current use. Such verifications have been made for a number of small molecules including methylthiirane, ${ }^{5}$ methyloxirane, ${ }^{6,13}$ trans-2,3-dimethyloxirane, ${ }^{7,11,13}$ trans-2,3-dimethylthiirane, ${ }^{11,12}$ alanine, ${ }^{8,9}$ tartaric acid $-d_{0}{ }^{10}$ and tartaric acid $-d_{4}{ }^{10}$ It is necessary to verify the theoretical predictions for a statistically significant number of molecules so that premature conclusions can be avoided.

In this article we report and analyze the experimental and theoretical depolarized ROA spectra for ( $R$ )-( + )-3-methylcyclohexanone. This study provides not only a rigorous test for the validity of the ab initio theoretical model currently used for ROA intensity calculations but also a detailed vibrational analysis and assignments for 3-methylcyclohexanone.

## Methods

The ROA spectra were obtained on a right-angle scattering ROA spectrometer developed at Glasgow. This instrument is slightly different from the $180^{\circ}$ backscattered ROA spectrometer reported earlier. ${ }^{32}$ The incident $\mathrm{Ar}^{+}$laser beam at 488 nm with $\sim 800-\mathrm{mW}$ power at the sample was modulated between right and left circular polarization states using a KD*P electrooptic modulator at $\sim 1 / 3 \mathrm{~Hz}$. The $90^{\circ}$ depolarized light wth linear polarization parallel to the scattering plane was collected and dispersed onto a backthinned, thermoelectrically cooled CCD detector (Wright Instruments). A $0.25-\mathrm{mm}$ spectrograph (JY HR250S) with a 1800 -grooves $/ \mathrm{mm}$ grating was used for spectral dispersion, with a resolution of $2.4 \mathrm{~cm}^{-1}$ at 500 nm using the $488-\mathrm{nm}$ excitation. Samples (Aldrich) were distilled twice and held in a cell ( $5-\mathrm{mm}$ pathlength, 2 mm wide, and 10 mm high) made of fused quartz. The light scattered during left circular polarization excitation was subtracted from that during the right circular polarization excitations to give the depolarized ROA spectrum, $I_{z}-I_{z}$. The instrument calibration and sensitivity are as detailed in ref 32. The depolarized Raman and ROA spectra are shown in Figure 1. For comparison with the theoretical predictions, the normalized circular intensity difference, ${ }^{1.33} \Delta_{z}=\left(I_{z}-I_{z}\right) /\left(I_{z}+I_{z}\right)$ will be used.

All theoretical calculations were done with $6-31 \mathrm{G}$ and $6-31 \mathrm{G}^{*}$ basis
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Figure 2. Ab initio theoretical depolarized ROA (bottom two) and Raman (top three) spectra for ( $R$ )-3-methylcyclohexanone. The corresponding experimental spectra for ( + )-3-methylcyclohexanone are displayed in the middle (labeled expt). The theoretical spectra were simulated with Lorentzian band shapes and a $10-\mathrm{cm}^{-1}$ half width after multiplying the theoretical frequencies by 0.9 to bring them closer to the experimental values. The theoretical intensities were multiplied by a constant to bring them to the same scale as that of the corresponding experimental values. The scales for $I^{R}+I^{L}$ and $I^{R}-I^{L}$ spectra differ by $10^{3}$, and the spectra are shifted from each other for clarity in the display.
sets. ${ }^{34}$ In the former basis set, the inner shell functions are expressed as linear combinations of six gaussian functions and the valence shell is split into two, one expressed with three gaussians and the second with one gaussian function. The 6-31 $\mathrm{G}^{*}$ basis set included, in addition, d-functions for C and O . For the ROA calculations the optical activity tensors in Cartesian displacement coordinates were evaluated with the 6-31G basis set and these tensors were converted to the normal coordinate space using the normal coordinates obtained from $6-31 \mathrm{G}$ as well as $6-31 \mathrm{G}^{*}$ basis sets. The latter calculation involving $6-31 \mathrm{G}^{*}$ normal coordinates and $6-31 \mathrm{G}$ Cartesian optical activity tensors is designated as $6-31 \mathrm{G}^{*} / 6-31 \mathrm{G}$. The quantities involved in these calculations are given as follows:

$$
\begin{equation*}
\Delta_{z}=\frac{I_{z}^{\mathrm{R}}-I_{z}^{L}}{I_{z}^{\mathrm{R}}+I_{z}^{L}}=\frac{24\left(\gamma^{2}-\delta^{2} / 3\right)}{12 c \beta^{2}} \tag{1}
\end{equation*}
$$

where

$$
\begin{gather*}
\gamma^{2}=1 / 2\left[3 \frac{\partial \alpha_{\alpha \beta}}{\partial Q} \frac{\partial G_{\alpha \beta}^{\prime}}{\partial Q}-\frac{\partial \alpha_{\alpha \alpha} \partial G_{\beta \beta}{ }^{\prime}}{\partial Q \partial Q}\right]  \tag{2}\\
\delta^{2}=\omega / 2 \frac{\partial \alpha_{\alpha \beta} \partial A_{\gamma \delta \beta}}{\partial Q \partial Q} \epsilon_{\alpha \gamma \delta}  \tag{3}\\
\beta^{2}=1 / 2\left[3 \frac{\partial \alpha_{\alpha \beta} \partial \alpha_{\alpha \beta}}{\partial Q \partial Q}-\frac{\partial \alpha_{\alpha \alpha} \partial \alpha_{\beta \beta}}{\partial Q \partial Q}\right] \tag{4}
\end{gather*}
$$

Here, $\left(\partial \alpha_{\alpha \beta} / \partial Q\right)=\sum_{A}\left(\partial \alpha_{\alpha \beta} / \partial X_{A}\right)\left(\partial X_{A} / \partial Q\right)$ with similar expressions for ( $\partial G_{\alpha \beta^{\prime}} / \partial Q$ ) and ( $\partial A_{\gamma \delta \beta} / \partial Q$ ). The ( $\partial X_{A} / \partial Q$ ) values represent atomic Cartesian displacements in a given normal mode $Q$ and were obtained
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Table I. Vibrational Raman Properties of ( $R$ )-(+)-3-Methylcyclohexanone ${ }^{a}$

| 6-31G |  |  |  |  | 6-31G* |  | 6-31G*/6-31G |  |  | 6-316* |  | Experiment |  | Assignment ${ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { mode } \\ & \text { no. } \end{aligned}$ | $\overline{\mathrm{v}}$ ( $\left.\mathrm{cm}^{-5}\right)^{\text {c }}$ | $45 \bar{\alpha}^{2}+7 \beta^{2}$ | $p$ | $\Delta_{2} \times 10^{4}$ | $\overline{\text { v }}$ | scaled | $45 \bar{\alpha}^{2}+7 \beta^{2}$ | $p$ | $\Delta_{2} \times 10^{4}$ | $45 \bar{\alpha}^{2}+7 \beta^{2}$ | p | $\overline{\text { v }}$ | $\Delta_{2} \times 10^{4}$ |  |
| 13 | 1910 | 16.0 | 0.54 | 0.5 | 2019 | 1817 | 17.1 | 0.54 | 0.4 | 15.1 | 0.57 | 1710 | 1.7 | $\mathrm{C}=0 \mathrm{str}$ |
| 14 | 1659 | 13.8 | 0.73 | 1.2 | 1650 | 1485 | 5.9 | 0.73 | 2.8 | 5.1 | 0.71 |  |  | $\mathrm{C}_{\beta} \cdot \mathrm{H}_{2}$ scissor $+\mathrm{C}_{\gamma} \mathrm{H}_{2}$ scissor |
| 15 | 1657 | 24.7 | 0.75 | 0.4 | 1644 | 1480 | 21.4 | . 0.74 | -0.2 | 17.8 | 0.74 | 1459 | 2.4 | asym $\mathrm{CH}_{3}$ bend |
| 16 | 1656 | 18.7 | 0.75 | 0.0 | 1644 | 1480 | 21.6 | 0.75 | 0.1 | 18.1 | 0.75 |  |  | asym $\mathrm{CH}_{3}$ bend |
| 17 | 1651 | 1.2 | 0.66 | -9.4 | 1638 | 1474 | 4.8 | 0.75 | -0.5 | 3.9 | 0.75 |  |  | $\mathrm{C}_{\gamma} \mathrm{H}_{2}$ scissor $+\mathrm{C}_{\beta} \mathrm{H}_{2}$ scissor |
| 18 | 1633 | 7.9 | 0.74 | -0.0 | 1620 | 1458 | 8.2 | 0.75 | -0.3 | 7.0 | 0.74 |  |  | $\mathrm{C}_{\alpha} \cdot \mathrm{H}_{2}$ scissor $+\mathrm{Ca}_{\mathrm{a}} \mathrm{H}_{2}$ scissor $+\mathrm{C}_{\gamma} \mathrm{H}_{2}$ scissor |
| 19 | 1625 | 13.9 | 0.75 | 0.5 | 1613 | 1452 | 17.1 | 0.75 | 0.8 | 14.7 | 0.75 | 1423 | -3.7 | $\mathrm{C}_{\alpha} \mathrm{H}_{2}$ scissor $+\mathrm{C}_{\alpha} \mathrm{H}_{2}$ scissor |
| 20 | 1580 | 2.0 | 0.73 | 0.2 | 1567 | 1410 | 1.2 | 0.70 | 3.0 | 1.1 | 0.71 |  |  | sym $\mathrm{CH}_{3}$ bend |
| 21 | 1538 | 2.7 | 0.65 | 0.4 | 1547 | 1392 | 4.4 | 0.69 | 0.4 | 3.9 | 0.66 | 1363 | -22.9 | $\mathrm{C}_{\gamma} \mathrm{H}_{2}$ wag $+\mathrm{C}_{\beta} \mathrm{H}$ bend $+\mathrm{C}_{\beta}-\mathrm{C}_{\gamma} \mathrm{str}$ |
| 22 | 1525 | 1.9 | 0.73 | 0.5 | 1519 | 1367 | 7.2 | 0.74 | 0.7 | 5.7 | 0.75 |  |  | $\mathrm{C}_{\beta} \mathrm{H}_{2}$ wag $+\mathrm{C}_{\beta} \mathrm{H}$ bend |
| 23 | 1510 | 14.8 | 0.75 | -0.8 | 1514 | 1363 | 5.6 | 0.75 | -3.5 | 4.5 | 0.75 | 1333 | -20.2 | $\mathrm{C}_{\beta} \mathrm{H}$ bend $+\mathrm{C}_{\beta} \cdot \mathrm{H}_{2}$ wag |
| 24 | 1493 | 6.6 | 0.73 | -0.8 | 1493 | 1344 | 6.0 | 0.71 | 0.3 | 4.5 | 0.73 |  |  | $\mathrm{C}_{\alpha} \cdot \mathrm{H}_{2}$ wag $+\mathrm{C}_{\beta} \cdot \mathrm{H}_{2}$ twist $+\mathrm{OC}-\mathrm{C}_{\alpha}$, st |
| 25 | 1488 | 1.7 | 0.75 | -4.7 | 1469 | 1322 | 4.8 | 0.75 | -1.3 | 4.1 | 0.75 | 1314 | -10.9 | $\mathrm{C}_{9} \mathrm{H}_{2}$ wag $+\mathrm{C}_{\beta} \mathrm{H}$ bend |
| 26 | 1449 | 7.2 | 0.75 | 1.7 | 1436 | 1292 | 4.8 | 0.73 | 2.9 | 3.6 | 0.74 | 1302 | +9.0 | $\mathrm{C}_{\alpha} \mathrm{H}_{2}$ wag $+\mathrm{C}_{\beta} \mathrm{H}$ bend |
| 27 | 1430 | 5.4 | 0.75 | 2.0 | 1411 | 1270 | 9.7 | 0.75 | -1.2 | 8.1 | 0.75 | 1265 | -14.1 | $\mathrm{C}_{\gamma} \mathrm{H}_{2}$ twist $+\mathrm{C}_{\alpha} \mathrm{H}_{2}$ twist $+\mathrm{C}_{\alpha}-\mathrm{H}_{2}$ twist |
| 28 | 1388 | 7.0 | 0.75 | -1.5 | 1369 | 1232 | 9.0 | 0.74 | -0.3 | 7.7 | 0.74 |  |  | $\mathrm{C}^{2} \cdot \mathrm{H}_{2}$ twist $+\mathrm{C}_{\alpha} \mathrm{H}_{2}$ twist |
| 29 | 1385 | 6.6 | 0.74 | 0.2 | 1360 | 1224 | 2.5 | 0.75 | -2.3 | 2.1 | 0.75 | 1223 | 6.3 | $\mathrm{C}_{\mathrm{c}} \mathrm{H}_{2}$ twist $+\mathrm{C}_{\alpha} \cdot \mathrm{H}_{2}$ wag $+\mathrm{C}_{\alpha} \mathrm{H}_{2}$ wag + asym $\mathrm{C}=\mathrm{O}$ bend |
| 30 | 1352 | 11.6 | 0.75 | -1.4 | 1345 | 1211 | 12.0 | 0.75 | -0.8 | 9.8 | 0.75 | 1200 | 10.2 | $\mathrm{C}_{\beta} \cdot \mathrm{H}_{2}$ twist $+\mathrm{C}_{\gamma} \mathrm{H}_{2}$ wag |
| 31 | 1277 | 4.0 | 0.17 | 11.9 | 1261 | 1135 | 4.1 | 0.14 | 15.2 | 3.1 | 0.14 | 1175 | 39.1 | $\mathrm{C}_{\alpha} \mathrm{H}_{2}$ rock $+\mathrm{C}_{\beta} \cdot \mathrm{H}_{2}$ rock $+\mathrm{CH}_{3}$ rock |
| 32 | 1244 | 3.6 | 0.73 | -0.1 | 1240 | 1116 | 3.5 | 0.72 | 0.4 | 2.8 | 0.72 | 1115 | -11.5 | $\mathrm{CH}_{3} \mathrm{rock}+\mathrm{C}_{\alpha}-\mathrm{C}_{\beta} \mathrm{str}+\mathrm{C}_{\beta}-\mathrm{C}_{\gamma} \mathrm{St}$ |
| 33 | 1196 | 8.4 | 0.70 | 1.2 | 1183 | 1065 | 9.1 | 0.67 | -2.2 | 8.0 | 0.67 | 1078 | -15.8 | $\mathrm{C}_{\beta}-\mathrm{CH}_{3} \mathrm{sr}$ |
| 34 | 1192 | 3.1 | 0.66 | -10.8 | 1162 | 1046 | 1.5 | 0.75 | 1.1 | 1.4 | 0.75 | 1053 | 4.7 | $\mathrm{C}_{\alpha} \mathrm{H}_{2}$ twist $+\mathrm{C}_{\alpha} \mathrm{H}_{2}$ twist $+\mathrm{C}_{\gamma} \mathrm{H}_{2}$ twist $+\mathrm{C}_{\beta} \mathrm{H}$ bend |
| 35 | 1149 | 4.6 | 0.73 | -0.2 | 1132 | 1019 | 6.1 | 0.74 | -0.4 | 5.1 | 0.74 | 1023 | -17.1 | $\mathrm{C}_{\beta}$ - $\mathrm{C}_{\gamma}$ str $+\mathrm{C}_{\alpha}$-- $\mathrm{C}_{\beta}$, str |
| 36 | 1085 | 1.4 | 0.66 | -0.8 | 1061 | 955 | 1.5 | 0.69 | -1.5 | 1.3 | 0.69 |  |  | $\mathrm{CH}_{3}$ rock $+\mathrm{C}_{\beta} \mathrm{H}$ bend $+\mathrm{C}_{\beta} \cdot \mathrm{H}_{2}$ rock |
| 37 | 1068 | 8.7 | 0.73 | 2.4 | 1054 | 949 | 8.6 | 0.73 | 2.4 | 7.2 | 0.74 | 971 | 31.8 | $\mathrm{CH}_{3}$ rock $+\mathrm{C}_{\beta}-\mathrm{C}_{\gamma}$ str $+\mathrm{C}_{\alpha} \cdot \mathrm{C}_{\beta} \cdot \mathrm{C}_{\gamma}$ bend $+\mathrm{C}_{\alpha} \cdot{ }^{-} \mathrm{C}_{\beta}$, str |
| 38 | 1048 | 8.0 | 0.67 | -2.0 | 1037 | 933 | 8.1 | 0.65 | -2.2 | 6.5 | 0.65 | 945 | -17.6 | $\mathrm{C}^{\prime} \cdot \mathrm{C}^{\prime} \cdot \mathrm{srr}+\mathrm{C}_{\beta} \cdot \mathrm{H}_{2}$ rock $+\mathrm{CH}_{3}$ rock $+\mathrm{C}_{\alpha} \mathrm{H}_{2}$ rock |
| 39 | 974 | 1.2 | 0.70 | 3.5 | 960 | 864 | 0.9 | 0.45 | 12.2 | 0.8 | 0.43 | 888 | -13.5 | $\mathrm{C}_{\beta}-\mathrm{C}_{\gamma} \mathrm{str}+\mathrm{C}_{\alpha}-\mathrm{C}_{\beta^{\prime}} \mathrm{sr}+\mathrm{C}_{\alpha} \mathrm{H}_{2}$ rock $+\mathrm{C}_{\gamma} \mathrm{H}_{2}$ rock |
| 40 | 956 | 2.8 | 0.26 | 1.5 | 950 | 855 | 2.8 | 0.30 | -0.8 | 2.2 | 0.29 | 870 | -20.4 | $\mathrm{C}_{\gamma} \mathrm{H}_{2}$ rock $+\mathrm{C}_{\alpha}-\mathrm{C}_{\beta} \cdot$ str $+\mathrm{C}_{\beta}-\mathrm{C}_{\gamma} \mathrm{str}+\mathrm{C}_{\alpha} \mathrm{H}_{2}$ rock |
| 41 | 938 | 2.7 | 0.35 | 4.3 | 915 | 824 | 3.1 | 0.36 | 5.2 | 2.9 | 0.36 | 833 | 11.7 | $\mathrm{C}_{\alpha} \cdot \mathrm{H}_{2}$ rock $+\mathrm{C}-\mathrm{C}_{\alpha} \mathrm{srr}+\mathrm{C}_{\alpha} \mathrm{H}_{2}$ rock $+\mathrm{CH}_{3}$ rock |
| 42 | 888 | 1.0 | 0.23 | -9.4 | 883 | 795 | 1.4 | 0.20 | -7.3 | 1.0 | 0.24 | 809 | -17.9 | $\mathrm{C}_{\beta}-\mathrm{C}_{\gamma} \mathrm{str}+\mathrm{C}-\mathrm{C}_{\alpha} \mathrm{str}+\mathrm{C}-\mathrm{C}_{\alpha}-\mathrm{str}+\mathrm{C}_{\alpha}-\mathrm{C}_{\beta} \mathrm{str}$ |
| 43 | 831 | 11.4 | 0.18 | 0.4 | 821 | 739 | 10.7 | 0.19 | -0.0 | 9.7 | 0.18 | 752 | -1.9 | $\mathrm{C}_{\beta} \cdot \mathrm{H}_{2}$ rock $+\mathrm{C}-\mathrm{C}^{\prime}{ }^{\prime} \mathrm{str}+\mathrm{C}_{\beta}-\mathrm{C}_{\gamma} \mathrm{str}+\mathrm{C}_{\alpha} \mathrm{H}_{2}$ rock |
| 44 | 693 | 12.0 | 0.07 | -3.0 | 692 | 623 | 11.8 | 0.06 | -3.4 | 10.2 | 0.06 | 642 | -20.5 | $\mathrm{C}=0$ out-of-plane bend $+\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ str |
| 45 | 558 | 2.1 | 0.38 | -10.3 | 555 | 500 | 2.0 | 0.47 | -7.4 | 1.4 | 0.40 | 516 | -36.6 | $\mathrm{C}=\mathrm{O}$ in-plane bend $+\mathrm{C}_{\alpha} \mathrm{C}_{3} \mathrm{C}\left(\mathrm{H}_{3}\right)$ bend |
| 45 | 533 | 1.7 | 0.56 | 9.2 | 526 | 473 | 1.8 | 0.50 | 7.3 | 1.4 | 0.46 | 490 | 37.4 | $\mathrm{C}_{\alpha} \cdot \mathrm{C}_{\beta} \cdot \mathrm{C}_{\gamma}$ bend $+\mathrm{C}_{\beta} \cdot \mathrm{C}_{\gamma} \mathrm{C}_{\beta}$ bend |
| 47 | 472 | 1.6 | 0.32 | -0.3 | 464 | 418 | 1.7 | 0.28 | -0.1 | 1.3 | 0.25 | 439 | 0.4 | $\mathrm{C}_{\alpha} \mathrm{CC}_{\alpha^{\prime}}$ bend $+\mathrm{C}_{\gamma} \mathrm{C}_{\beta} \mathrm{C}\left(\mathrm{H}_{3}\right)$ bend $+\mathrm{C}_{\alpha} \mathrm{H}_{2}$ rock |
| 48 | 438 | 4.0 | 0.37 | 1.4 | 427 | 384 | 3.7 | 0.38 | 1.7 | 3.2 | 0.37 | 400 | 10.8 | $\mathrm{C}_{\alpha} \cdot \mathcal{C}_{\beta} \cdot \mathrm{C}_{\gamma}$ bend $+\mathrm{C}_{\beta} \mathrm{C}_{\alpha} \mathrm{C}$ bend $+\mathrm{C}_{\beta} \cdot \mathrm{C}_{\alpha} \cdot \mathrm{C}$ bend |
| 49 | 419 | 1.2 | 0.60 | 0.5 | 411 | 370 | 1.1 | 0.67 | -0.3 | 0.8 | 0.65 | 386 | -13.2 | $\mathrm{C}_{\alpha} \mathrm{CC}_{\alpha^{\prime}}$ bend $+\mathrm{C}_{\beta} \mathrm{C}_{\alpha} \mathcal{C}$ bend $+\mathrm{C}_{\beta} \mathrm{C}_{\gamma} \mathrm{C}_{\beta}$, bend |
| 50 | 320 | 0.2 | 0.63 | -8.5 | 316 | 284 | 0.1 | 0.63 | -8.9 | 0.1 | 0.57 | 300 | -21.4 | $\mathrm{C}\left(\mathrm{H}_{3}\right) \mathrm{C}_{\beta} \mathrm{C}_{\gamma}$ bend $+\mathrm{C}\left(\mathrm{H}_{3}\right) \mathrm{C}_{\beta} \mathrm{C}_{\alpha}$ bend |
| 51 | 270 | 0.2 | 0.72 | -10.0 | 270 | 243 | 0.2 | 0.70 | -9.2 | 0.2 | 0.71 | 255 | -60.5 | $\mathrm{CC}_{\alpha} \mathrm{C}_{\beta} \mathrm{C}_{\boldsymbol{\gamma}}$ torsion $+\mathrm{CC}_{\alpha}-\mathrm{C}_{\beta}-\mathrm{C}_{\gamma}$ torsion |
| 52 | 247 | 0.0 | 0.72 | -3.5 | 253 | 228 | 0.0 | 0.68 | -6.4 | 0.0 | 0.67 | 218 |  | $\mathrm{CH}_{3}$ torsion |
| 53 | 140 | 0.1 | 0.75 | 8.8 | 139 | 125 | 0.1 | 0.75 | 8.6 | 0.1 | 0.75 | 142 | 22.3 | $\mathrm{CC}_{\alpha} \mathrm{C}_{\beta} \mathrm{C}_{\boldsymbol{\gamma}}$ torsion $+\mathrm{CC}_{\alpha} \mathrm{C}_{\beta} \mathrm{C}_{\boldsymbol{\gamma}}$ torsion |
| 54 | 103 | 0.6 | 0.75 | 1.7 | 102 | 92 | 0.6 | 0.74 | 1.7 | 0.4 | 0.75 | 125 |  | $\mathrm{CC}_{\alpha} \mathrm{C}_{\beta}$ bend $+\mathrm{CC}_{\alpha} \cdot \mathrm{C}_{\beta} \cdot$ bend $+\mathrm{C}=0$ out-of-plane bend |

${ }^{a}$ Raman intensity parameters are expressed as $45 \bar{\alpha}^{2}+7 \beta^{2}$, in ( $\AA^{4} / \mathrm{amu}$ ). $\rho$ is the depolarization ratio defined as $3 \beta^{2} /\left(45 \bar{\alpha}^{2}+4 \beta^{2}\right)$. In the 6-31G*/6-3IG calculation, normal modes obtained with the $6-31 \mathrm{G}^{*}$ basis set and Cartesian polarizability derivative tensors obtained with the 6-31G basis set were used. In addition to the experimental bands listed, weak bands at $\sim 350,362,549,675,786,1574,1611,1639,1676,1713$, and 1746 $\mathrm{cm}^{-1}$ are apparent in the experimental Raman spectrum. These bands are considered to be due to nonfundamental modes. ${ }^{b}$ The assignments were derived from the potential energy distribution and (or) displacements in internal coordinates. These descriptions depend on the choice of internal coordinates used, which is arbitrary. The internal symmetry coordinates employed are as follows: 20 bond stretches, $16 \mathrm{CH}_{2}$ bends (four per $\mathrm{CH}_{2}$ group representing scissors, twist, rock, and wagging motions), 2 methine bends, $2 \mathrm{C}-\mathrm{C}\left(\mathrm{H}_{3}\right)$ bends, $6 \mathrm{CH}_{3}$ bends (representing one symmetric, two asymmetric, two rock, and one torsional motion), $2 \mathrm{C}=0$ bends (one in-plane and one out-of-plane motion), 5 ring bends (one each at $\mathrm{C}, \mathrm{C} \alpha, \mathrm{C} \alpha^{\prime}$, $\mathrm{C} \beta^{\prime}$, and $\mathrm{C} \gamma$ ), and a ring torsion.
with the 6-31G and 6-31G* basis sets. The derivatives $\partial \alpha_{\alpha \beta} / \partial \boldsymbol{X}_{A}, \partial G_{\alpha \beta^{\prime}} /$ $\partial \boldsymbol{X}_{A}$, and $\partial A_{\alpha \beta \gamma} / \partial \boldsymbol{X}_{A}$ were obtained numerically by evaluating the tensors $\alpha_{\alpha \beta}, G_{\alpha \beta^{\prime}}$, and $A_{\alpha \beta \gamma}$ at the equilibrium geometries and at geometries displaced by 0.005 A along each atomic Cartesian coordinate. The need for this numerical method arises from the unavailability at the present time of an analytic procedure for evaluating $\partial G_{\alpha \beta^{\prime}} / \partial \boldsymbol{X}_{A}$. The procedure for obtaining $G_{\alpha \beta^{\prime}}$ is based on the static limit approximation and is due to Amos ${ }^{35}$ as implemented in the CADPAC program, ${ }^{36}$ which simultaneously evaluates $\alpha_{\alpha \beta}$ and $A_{\alpha \beta \gamma}$. All calculations were done at the fully optimized geometries for the chair conformer with the methyl group in an equatorial position. The vibrational frequencies, normal modes, and Raman intensities were also obtained at the same geometries.
The theoretical Raman and ROA spectra were simulated with Lorentzian band shapes and are compared to the corresponding experimental spectra in Figure 2. The normalized circular intensity differences $\Delta_{z}$ are compared in Table I. The theoretical vibrational frequencies,

[^2]Raman intensities, and mode descriptions are also summarized in Table 1. Three-dimensional displays, similar to those in ref 28 , for the $6-31 \mathrm{G}^{*}$ modes were generated by adopting the ORTEP program ${ }^{37}$ as in the earlier work. ${ }^{38}$ These are not presented here but can be obtained from the authors. The theoretical frequencies were multiplied by 0.9 to bring them closer to the experimental values. The frequencies obtained with the $6-31 \mathrm{G}^{*}$ basis set and scaled by 0.9 will be used in the discussion, unless specified otherwise.

## Results and Discussion

Molecular Structure. The molecular structure of 3-methylcyclohexanone has not been determined experimentally. Previous theoretical studies ${ }^{22-30.31 d-8}$ on 3-methylcyclohexanone have used
(37) Johnson, C. K. ORTEP: A Fortran thermal ellipsoid plot program for crystal structure illustrations; Oak Ridge National Laboratory: Oak Ridge, TN, 1976.
(38) Polavarapu, P. L.; Pickard, S. T.; Smith, H. E.; Black, T. M.; Rauk, A.; Yang, D. J. Am. Chem. Soc. 1991, 113, 9747 . Hess, B. A., Jr.; Cha, J. K.; Schaad, L. J.; Polavarapu, P. L. J. Org. Chem. 1992, 57, 6367.
either the idealized ${ }^{31 d}$ bond lengths and angles or those approximated for related cyclohexanones. $31 \mathrm{c}, \mathrm{g}$ With the idealized structural parameters, ab initio studies using a minimal basis set predicted ${ }^{31 e}$ the energy for the chair conformer with the methyl group in an equatorial position to be favorable, over that with the methyl group in an axial position, by $\sim 3 \mathrm{kcal} / \mathrm{mol}$. Experimental circular dichroism ${ }^{31 a, b}$ and microwave studies ${ }^{31 \mathrm{c}}$ also suggested that the chair form with the methyl group in an equatorial position is preferred and that the populations of other conformers (axial methyl group and twisted ring) are small. On the basis of these previous conclusions we assumed that the chair conformer of 3 -methylcyclohexanone with the methyl group in an equatorial position is predominant and optimized the structure of this conformer. The $6-31 \mathrm{G}^{*}$ energy of this conformer at the fully optimized geometry is -346.9417 hartrees. The axial C-H bond lengths $\left(\mathrm{C}-\mathrm{H}_{\mathrm{a}}\right)$ are slightly longer than the equatorial $\mathrm{C}-\mathrm{H}$ bond lengths $\left(\mathrm{C}-\mathrm{H}_{e}\right): \mathrm{C}_{\alpha}-\mathrm{H}_{\mathrm{a}}=1.090, \mathrm{C}_{\alpha}-\mathrm{H}_{\mathrm{e}}=1.083, \mathrm{C}_{\beta}-\mathrm{H}_{\mathrm{a}}=1.090$, $\mathrm{C}_{\alpha}-\mathrm{H}_{\mathrm{a}}=1.089, \mathrm{C}_{\alpha}-\mathrm{H}_{\mathrm{e}}=1.083, \mathrm{C}_{\beta^{\prime}}-\mathrm{H}_{\mathrm{a}}=1.088, \mathrm{C}_{\beta^{\prime}}-\mathrm{H}_{\mathrm{e}}=$ $1.085, \mathrm{C}_{\gamma}-\mathrm{H}_{\mathrm{a}}=1.090, \mathrm{C}_{\gamma}-\mathrm{H}_{\mathrm{e}}=1.086 \AA\left(\mathrm{C}, \mathrm{C}_{\alpha}, \mathrm{C}_{\beta}, \mathrm{C}_{\gamma}, \mathrm{C}_{\beta^{\prime}}\right.$, and $\mathrm{C}_{\alpha^{\prime}}$ are, respectively, the carbon atoms at positions 1-6 of the ring). The heavy atom bond lengths are as follows: $\mathrm{C}-\mathrm{O}=1.19$, $\mathrm{C}-\mathrm{C}_{\alpha}=1.52, \mathrm{C}-\mathrm{C}_{\alpha}=1.52, \mathrm{C}_{\alpha}-\mathrm{C}_{\beta}=1.54, \mathrm{C}_{\alpha^{\prime}}-\mathrm{C}_{\beta^{\prime}}=1.54, \mathrm{C}_{\beta^{-}}$ $\mathrm{C}_{\gamma}=1.53, \mathrm{C}_{\beta^{\prime}}-\mathrm{C}_{\gamma}=1.53 \AA$. The heavy atom angles are as follows: $\mathrm{OCC}_{\alpha}=122^{\circ}, \mathrm{C}_{\alpha} \mathrm{CC}_{\alpha^{\prime}}=115^{\circ}, \mathrm{CC}_{\alpha} \mathrm{C}_{\beta}=112^{\circ}, \mathrm{CC}_{\alpha^{\prime}} \mathrm{C}_{\beta^{\prime}}$ $=111^{\circ}, \mathrm{C}_{\alpha} \mathrm{C}_{\beta} \mathrm{C}_{\gamma}=110^{\circ}, \mathrm{C}_{\alpha^{\prime}} \mathrm{C}_{\beta^{\prime}} \mathrm{C}_{\gamma}=112^{\circ}, \mathrm{C}_{\beta} \mathrm{C}_{\gamma} \mathrm{C}_{\beta^{\prime}}=112^{\circ}$, $\mathrm{C}_{\alpha} \mathrm{C}_{\beta} \mathrm{C}\left(\mathrm{H}_{3}\right)=111^{\circ}$. The HCH angles at $\alpha, \alpha^{\prime}, \beta^{\prime}$, and $\gamma$ positions, respectively, are $108^{\circ}, 108^{\circ}, 107^{\circ}$, and $107^{\circ}$. The ring torsional angles are as follows: $\tau\left(\mathrm{CC}_{\alpha} \mathrm{C}_{\beta} \mathrm{C}_{\gamma}\right)=-52^{\circ}, \tau\left(\mathrm{CC}_{\alpha} \mathrm{C}_{\beta} \mathrm{C}_{\gamma}\right)=52^{\circ}$, $\tau\left(\mathrm{OCC}_{\alpha} \mathrm{C}_{\beta}\right)=131^{\circ}, \tau\left(\mathrm{CC}_{\alpha} \mathrm{C}_{\beta} \mathrm{C}\left(\mathrm{H}_{3}\right)\right)=177^{\circ}$. Some of these structural parameters are significantly different from the ones previously used; for example, the $\mathrm{C}=\mathrm{O}$ bond length is $1.19 \AA$ as opposed to the assumed ${ }^{31 \mathrm{c}}$ value of $1.22 \AA$ and the $\mathrm{C}_{\alpha} \mathrm{CC}_{\alpha^{\prime}}$ angle is $115^{\circ}$ as opposed to the idealized ${ }^{31 \mathrm{~d}}$ value of $120^{\circ}$. A complete list of the structural parameters can be obtained from the authors.
Raman Spectra. The comparison of experimental and theoretical depolarized Raman spectra in Figure 2 indicates that the experimental spectrum is reproduced qualitatively well by both $6-31 \mathrm{G}$ and $6-31 \mathrm{G}^{*}$ basis set calculations. No major differences are evident among the predictions of 6.31 G and $6.31 \mathrm{G}^{*}$ basis sets. However, small differences in the relative intensities of the bands in the region around $1350 \mathrm{~cm}^{-1}$ are present in these two calculations, where the predicted relative intensities in the 6-31G calculation are closer to the observed ones. The relative Raman intensities obtained in the mixed $6-31 \mathrm{G}^{*} / 6-31 \mathrm{G}$ calculation are nearly identical to those in the $6-31 \mathrm{G}^{*}$ calculation, indicating that the Cartesian electric dipole polarizability derivative tensors are not influenced significantly by the addition of polarization functions to the 6-31G basis set. This observation is in accord with those reported earlier for other molecules. $6,7,13$

The experimental polarized Raman spectra for different isotopomers of 3 -methylcyclohexanone, namely 3 -methylcyclo-hexanone-3- $d_{1}, 3$-(methyl- $d_{3}$ )cyclohexanone, 3-methylcyclohex-anone-5,5- $d_{2}$, 3-methylcyclohexanone-4,4- $d_{2}$, and 3-methylcy-clohexanone- $2,2,6,6-d_{4}$, were reported by Freedman et al. ${ }^{28}$ in the $\sim 100-700-\mathrm{cm}^{-1}$ region. The quality of ab initio predictions can be tested further by comparing the ab initio predictions of Raman spectra for these isotopomers. The simulated spectra obtained with the $6-31 \mathrm{G}^{*}$ basis set are shown in Figure 3, and the frequency and intensity data are summarized in Table II. There are 11 modes below $700 \mathrm{~cm}^{-1}$ for these molecules. The experimental band positions corresponding to eight of these higher frequency modes, as reported by Freedman et al., ${ }^{28}$ are also summarized in Table II.

The experimental polarized Raman spectrum (not shown here) of 3 -methylcyclohexanone in the $100-700-\mathrm{cm}^{-1}$ region is similar to the corresponding depolarized Raman spectrum shown in Figures 1 and 2, except that the band at $642 \mathrm{~cm}^{-1}$ being strongly polarized has significantly larger intensity in the former. The


Figure 3. $A b$ initio theoretical polarized Raman spectra obtained with the 6-31G* basis set for (a) 3-methylcyclohexanone, (b) 3-methylcy-clohexanone-3- $d_{1}$, (c) 3-(methyl- $d_{3}$ )cyclohexanone, (d) 3 -methylcyclo-hexanone-5,5- $d_{2}$, (e) 3-methylcyclohexanone-4,4- $d_{2}$, and (f) 3-methyl-cyclohexanone- $2,2,6,6-d_{4}$. All spectra are on the same relative intensity scale but are shifted from each other for clarity. The 6-31G* frequencies were multiplied by 0.9 to bring them closer to the experimental values, and the spectra were simulated with Lorentzian band shapes and a $5-\mathrm{cm}^{-1}$ half width.
corresponding $6-31 \mathrm{G}^{*}$ theoretical mode with a scaled frequency of $632 \mathrm{~cm}^{-1}$ is also predicted to be strongly polarized with a depolarization ratio of only 0.06 . This mode has a major contribution from the out-of-plane $\mathrm{C}=\mathrm{O}$ bending motion. The internal coordinate coupling associated with this mode varies in the isotopomers of 3 -methylcyclohexanone, and this variation causes the intensity and frequency associated with this mode to change. It is of interest to note that the predicted frequency of this mode decreases in the order of isotopomers shown in Figure 3 , and an identical order of frequency shifts was observed ${ }^{28}$ for the corresponding experimental bands (see Table II). The intensity of this mode is not significantly influenced in the $-3-d_{1}$ and -(methyl- $d_{3}$ ) isotopomers but decreases by nearly half in the $-5,5-d_{2}$ isotopomer and then increases from that value by $\sim 1.5$ in the $-4,4-d_{2}$ and $-2,2,6,6-d_{4}$ isotopomers. Identical relative trends were found ${ }^{28}$ for the corresponding experimental Raman bands.

In the $300-500-\mathrm{cm}^{-1}$ region, the spectral pattern seen for the parent molecule is retained, with minor frequency shifts, for the $-3-d_{1}$ and -(methyl $-d_{3}$ ) isotopomers. One point of interest here is that the two modes with scaled frequencies of 370 and $384 \mathrm{~cm}^{-1}$ for the parent molecule give rise to resolved bands in the simulated spectrum, but for the-(methyl $-d_{3}$ ) isotopomer they are predicted to be closer in frequency, at 364 and $372 \mathrm{~cm}^{-1}$, resulting in poorly resolved bands in the simulated spectrum. This predicted pattern is in agreement with that observed in the experimental spectra. ${ }^{28}$ The spectral pattern in this region is predicted to be significantly different for the $-4,4-d_{2}$ and $2,2,6,6-d_{4}$ isotopomers, and the predicted patterns for these molecules are nearly identical to those seen in the experimental spectra. ${ }^{28}$ One minor discrepancy

Table II. Vibrational Frequencies and Raman Intensities for Isotopomers of 3-Methylcyclohexanone ${ }^{a}$

| -d ${ }_{0}$ |  |  |  |  | $-3-d_{1}$ |  |  |  |  | methyl- $d_{3}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\bar{\nu}\left(\mathrm{cm}^{-1}\right)$ |  |  | Raman |  | $\bar{\nu}\left(\mathrm{cm}^{-1}\right)$ |  |  | Raman |  | $\bar{\nu}\left(\mathrm{cm}^{-1}\right)$ |  |  | Raman |  |
| 6-31G* | scaled | expt | $45 \bar{\alpha}^{2}+7 \beta^{2}$ | $\rho$ | 6-31G* | scaled | expt | $45 \bar{\alpha}^{2}+7 \beta^{2}$ | $\rho$ | 6-31G* | scaled | expt | $45 \bar{\alpha}^{2}+7 \beta^{2}$ | $\rho$ |
| 692 | 623 | 642 | 10.0 | 0.06 | 690 | 621 | 639 | 10.0 | 0.06 | 682 | 614 | 635 | 10.9 | 0.07 |
| 555 | 500 | 514 | 1.4 | 0.40 | 553 | 498 | 511 | 1.3 | 0.46 | 547 | 492 | 506 | 1.3 | 0.59 |
| 526 | 473 | 490 | 1.4 | 0.40 | 524 | 472 | 488 | 1.3 | 0.45 | 519 | 467 | 485 | 1.1 | 0.50 |
| 464 | 418 | 439 | 1.3 | 0.25 | 462 | 416 | 437 | 1.3 | 0.28 | 454 | 409 | 429 | 1.1 | 0.50 |
| 427 | 384 | 398 | 3.2 | 0.37 | 423 | 381 | 395 | 3.2 | 0.36 | 413 | 372 | 383 | 3.2 | 0.38 |
| 411 | 370 | 388 | 0.8 | 0.65 | 408 | 367 | 385 | 0.8 | 0.71 | 404 | 364 | 383 | 1.1 | 0.27 |
| 316 | 284 | 299 | 0.1 | 0.57 | 313 | 282 | 295 | 0.1 | 0.57 | 288 | 259 | 270 | 0.0 | 0.47 |
| 270 | 243 | 259 | 0.2 | 0.71 | 269 | 242 | 258 | 0.2 | 0.71 | 259 | 233 | 248 | 0.2 | 0.75 |
| 253 | 228 |  | 0.0 | 0.67 | 253 | 228 |  | 0.0 | 0.66 | 184 | 166 |  | 0.0 | 0.74 |
| 139 | 125 |  | 0.1 | 0.75 | 138 | 124 |  | 0.1 | 0.75 | 133 | 120 |  | 0.1 | 0.74 |
| 102 | 92 |  | 0.4 | 0.75 | 101 | 91 |  | 0.4 | 0.75 | 100 | 90 |  | 0.4 | 0.75 |
| $-5,5-d_{2}$ |  |  |  |  | $-4,4-d_{2}$ |  |  |  |  | $-2,2,6,6-d_{4}$ |  |  |  |  |
| $\bar{\nu}\left(\mathrm{cm}^{-1}\right)$ |  |  | Raman |  | $\bar{\nu}\left(\mathrm{cm}^{-1}\right)$ |  |  | Raman |  | $\bar{\nu}\left(\mathrm{cm}^{-1}\right)$ |  |  | Raman |  |
| 6-31G* | scaled | expt | $45 \bar{\alpha}^{2}+7 \beta^{2}$ | $\rho$ | 6-31G* | scaled | expt | $45 \bar{\alpha}^{2}+7 \beta^{2}$ | $\rho$ | 6-31G* | scaled | expt | $45 \bar{\alpha}^{2}+7 \beta^{2}$ | $\rho$ |
| 677 | 609 | 625 | 6.1 | 0.08 | 672 | 605 | 620 | 8.9 | 0.06 | 660 | 594 | 613 | 9.2 | 0.08 |
| 550 | 495 | 511 | 1.4 | 0.38 | 553 | 498 | 510 | 1.3 | 0.40 | 507 | 456 | 469 | 1.0 | 0.39 |
| 507 | 456 | 476 | 1.3 | 0.45 | 509 | 458 | 472 | 1.9 | 0.30 | 501 | 451 | 469 | 2.0 | 0.37 |
| 459 | 413 | 435 | 1.8 | 0.21 | 448 | 403 | 421 | 1.1 | 0.66 | 425 | 383 | 399 | 1.8 | 0.15 |
| 421 | 379 | 395 | 2.7 | 0.43 | 423 | 381 | 393 | 2.9 | 0.40 | 404 | 364 | 376 | 1.8 | 0.68 |
| 410 | 369 | 388 | 0.8 | 0.65 | 389 | 350 | 364 | 0.6 | 0.33 | 376 | 338 | 353 | 0.8 | 0.75 |
| 310 | 279 | 295 | 0.1 | 0.66 | 311 | 280 | 294 | 0.1 | 0.64 | 311 | 280 | 295 | 0.1 | 0.56 |
| 257 | 231 | 230 | 0.1 | 0.74 | 255 | 230 | 242 | 0.1 | 0.67 | 264 | 238 | 253 | 0.1 | 0.71 |
| 241 | 217 |  | 0.1 | 0.67 | 253 | 228 |  | 0.0 | 0.65 | 252 | 227 |  | 0.0 | 0.64 |
| 138 | 124 |  | 0.1 | 0.75 | 138 | 124 |  | 0.1 | 0.75 | 128 | 115 |  | 0.1 | 0.74 |
| 101 | 91 |  | 0.4 | 0.75 | 99 | 89 |  | 0.4 | 0.75 | 97 | 87 |  | 0.4 | 0.75 |

${ }^{a}$ Scaled frequencies were obtained by multiplying the 6-31G* frequencies by 0.9 . Raman intensity oparameters $\left(45 \bar{\alpha}^{2}+7 \beta^{2}\right)$ and the depolarization ratio ( $\rho$ ) were obtained with the $6-31 G^{*}$ basis set. The experimental frequencies are from ref 28.
is that the two modes of the $-2,2,6,6-d_{4}$ isotopomer with scaled frequencies of 376 and $399 \mathrm{~cm}^{-1}$ are predicted to have equal intensities, whereas the corresponding experimental bands at 364 and $383 \mathrm{~cm}^{-1}$ have unequal intensities with the former slightly less intense than the latter.

The two modes in the $200-300-\mathrm{cm}^{-1}$ region are predicted to be weak for all of the molecules considered here. The variations in frequencies and intensities of these modes among the isotopomers are similar to the corresponding variations seen in the experimental spectra.

Raman Optical Activity. The depolarized ROA spectrum of $(R)-(+)$-3-methylcyclohexanone presented here reproduces all of the major features reported several years ago using an older generation ROA instrument. ${ }^{39}$ A comparison of the experimental and theoretical ROA spectra (Figure 2) indicates that for a large number of bands the ROA signs observed for ( + )-3-methylcyclohexanone and those predicted for $(R)$-3-methylcyclohexanone are in agreement. As in the Raman spectra, there are no major differences among the ROA predictions obtained in the 6-31G and $6-31 \mathrm{G}^{*} / 6-31 \mathrm{G}$ calculations.

The correlation between the theoretical modes and the experimental bands, presented in Table I, is obtained from a consideration of the relative Raman intensities as well as the ROA signs. Due to the presence of a large number of vibrations for this molecule in the $100-1800-\mathrm{cm}^{-1}$ region, and since all of the ROA features associated with these vibrations may not be of general interest, the discussion will be restricted to those ROA features that have attracted attention in the literature. For the remaining ROA and Raman bands the reader can find the appropriate information in Table I.

Couplet in the $130-260-\mathrm{cm}^{-1}$ Region. The positive-negative ROA couplet observed in this region was thought to have ${ }^{26}$ a major contribution from the methyl torsion vibration. This was partly based on the assertion that the methyl torsion in methylcyclohexane occurs at $237 \mathrm{~cm}^{-1}$ and on the predictions of the
(39) Barron, L. D. J. Chem. Soc., Perkin Trans. 2 1977, 1074.
inertial model. ${ }^{40}$ The frequency range associated with the methyl torsion mode is supported by the present $a b$ initio calculations. The scaled $6-31 \mathrm{G}^{*}$ frequency for this mode is $228 \mathrm{~cm}^{-1}$. The present calculations indicate that the Raman intensity associated with the methyl torsion mode is not significant enough to be observed in the Raman spectrum. The weak Raman band present in the experimental spectrum at $218 \mathrm{~cm}^{-1}$ probably corresponds to this mode. Nevertheless, a moderate-size negative $\Delta_{z}$ value is predicted in the present calculations for this mode, and therefore it is possible to assume that the negative ROA in the experimental spectrum sloping toward the $255-\mathrm{cm}^{-1}$ band might be associated with the methyl torsion Raman band.
It is clear that the methyl torsion vibration has very weak Raman and ROA intensities. Therefore it is unlikely that the methyl torsion mode will serve as a useful marker for determining the absolute configuration in general, but for small molecules such as trans-2,3-dimethyloxirane and trans-2,3-dimethylthiirane, the methyl torsion ROA was indeed found to be useful. ${ }^{11,12}$ The present calculations suggest that, in the immediate vicinity of the methyl torsion band, the observed positive ROA at $142 \mathrm{~cm}^{-1}$ originates from a ring mode predicted to appear at an unscaled ab initio frequency of $139 \mathrm{~cm}^{-1}$ and the negative observed ROA at $255 \mathrm{~cm}^{-1}$ originates from another ring mode predicted to appear at an unscaled ab initio frequency of $270 \mathrm{~cm}^{-1}$. These two modes have larger contributions from the torsional motions around the $\mathrm{C}_{\alpha}-\mathrm{C}_{\beta}$ and $\mathrm{C}_{\alpha^{\prime}}-\mathrm{C}_{\beta^{\prime}}$ bonds. The normal mode for the unscaled $139-\mathrm{cm}^{-1}$ frequency has a significant contribution from $\mathrm{C}-\mathrm{CH}_{3}$ stretching but no significant $\mathrm{CCH}_{3}$ bending motion, unlike the mode description derived from the empirical force field calculation. ${ }^{28}$ It is of interest to note that in the experimental spectrum a neighboring negative ROA band at $300 \mathrm{~cm}^{-1}$ is predicted to originate from the bending of the methyl carbon atom (relative to the ring carbon atoms) and this mode has observable Raman intensity. Therefore, the $\mathrm{H}_{3} \mathrm{C}-\mathrm{C}-\mathrm{C}$ bending motion may serve

[^3]as a better ROA signature of the methyl group at the chiral center than the methyl torsion mode.

Couplet in the $380-410-\mathrm{cm}^{-1}$ Region. The observed negativepositive couplet, from the low-frequency side, is associated with the broader Raman band with a resolved low-frequency shoulder. The present calculations indicate that the two modes at 370 and $384 \mathrm{~cm}^{-1}$ are responsible for the observed Raman band and the associated ROA couplet. The negative portion of the couplet is not seen in the simulated spectrum, because of small magnitude, but the $370-\mathrm{cm}^{-1}$ mode is indeed predicted to have negative ROA (see Table I). Therefore the current predictions are in reasonable agreement with the observed Raman and ROA features, and the associated mode descriptions might be considered reliable. The $384-\mathrm{cm}^{-1}$ mode is essentially a ring-bending mode, and that at $370 \mathrm{~cm}^{-1}$ has significant contributions from the $\mathrm{C}_{\alpha} \mathrm{CC}_{\alpha^{\prime}}$ bending motion as well as ring-bending motions. Earlier analyses ${ }^{23,28}$ employing empirical force fields also attributed these two modes to ring-bending motions, but the internal coordinate couplings obtained in those calculations appear to be different from the ones obtained in the present $a b$ initio calculations (as deduced from the comparison of the present normal mode displays with those in ref 28).

Couplet in the $\mathbf{4 8 0}-\mathbf{5 2 0}-\mathrm{cm}^{-1}$ Region. The observed positivenegative couplet, from the low-frequency side, is correctly reproduced in the theoretical spectrum, as are the corresponding relative Raman intensities. The theoretical modes are predicted to occur at 473 and $500 \mathrm{~cm}^{-1}$, corresponding to the observed band positions of 490 and $516 \mathrm{~cm}^{-1}$, respectively. The former mode is due to a ring-bending mode and the latter due to the in-plane $\mathrm{C}=\mathrm{O}$ bending motion that is coupled with the bending motion of the methyl carbon atom (relative to the ring). The mode description for the $516-\mathrm{cm}^{-1}$ band is quite similar to that suggested by Barron and Clark. ${ }^{26}$ However, unlike the earlier prediction, there is no significant in-plane $\mathrm{C}=\mathrm{O}$ bending contribution to the $490-\mathrm{cm}^{-1}$ band. The prediction by Freedman and co-workers ${ }^{28}$ that the observed bands at 490 and $516 \mathrm{~cm}^{-1}$ are due to in- and out-of-phase combinations of in-plane $\mathrm{C}=\mathrm{O}$ bending with ring deformation is not supported by the present results. In this context it is of interest to note that the weak Raman and negative ROA sign characteristics predicted for the theoretical out-of-plane $\mathrm{C}=\mathrm{O}$ bending mode at $623 \mathrm{~cm}^{-1}$ correspond very nicely to the observed weak Raman and negative ROA observed at $642 \mathrm{~cm}^{-1}$.

Couplet in the $930-980-\mathrm{cm}^{-1}$ Region. The bisignate couplet observed in this region consists of a negative band at $945 \mathrm{~cm}^{-1}$ and a strong positive band at $971 \mathrm{~cm}^{-1}$. The ROA signs seen in the simulated spectrum agree with these signs. However, the relative theoretical ROA intensities of these two components are not in complete agreement with the experimental observation. The simulated spectrum shows nearly equal intensities for the bisignate couplet, whereas in the experimental spectrum the negative is about half the intensity associated with the positive component. There are three modes at 933,949 , and $955 \mathrm{~cm}^{-1}$ which are apparently responsible for the observed couplet. Two of these, at 949 and $955 \mathrm{~cm}^{-1}$, are due to the two methyl rocking modes with oppositely signed ROA of unequal intensity, and their close proximity results in significant cancellation; the positive ROA comes from what is left after cancellation. The negative ROA originates from the $933-\mathrm{cm}^{-1}$ mode that is due to a ring stretch coupled to the methylene and methyl group bending motions. These mode predictions are different from the earlier hypotheses which associated the bisignate couplet to the two methyl rocking modes. Although the present calculations predict these two modes to have opposite ROA signs, the facts that one of them has weak Raman and ROA and that they overlap significantly make it difficult to suggest that ROA associated with these two modes is resolved in the experimental spectrum.

The interpretation offered by Zimba et al. ${ }^{29}$ for the ROA couplet under discussion, however, raises some further questions. They
reported three ROA bands at 969,960 , and $946 \mathrm{~cm}^{-1}$ with positive, negative, and negative ROA signs, respectively. The presence of three bands here is supported by the present calculations as well as by the presence of three bands in this region of the infrared absorption and higher resolution Raman spectra. Two of the bands reported by Zimba et al. at 969 and $946 \mathrm{~cm}^{-1}$ probably correspond to the present experimental bands at 971 and 945 $\mathrm{cm}^{-1}$. The negative ROA band at $960 \mathrm{~cm}^{-1}$ does not have a counterpart in the present experimental spectrum and is most likely an ROA artifact. However, if their observation is correct, then the predicted order of the two methyl rocking modes in the present calculations has to be interchanged. The suggestion that their $946-\mathrm{cm}^{-1}$ band originates from the $\mathrm{C}-\mathrm{CH}_{3}$ stretch is not supported by the present results.

Other Couplets in the $1000-1500-\mathrm{cm}^{-1}$ Region. There are four closely spaced couplets clearly resolved in the experimental spectrum in this region. The origin of these couplets can be deduced from the corresponding theoretical predictions. The negative-positive-negative triplet in the $1020-1090-\mathrm{cm}^{-1}$ region appears to originate from the ring $\mathrm{C}-\mathrm{C}$ stretches, $\mathrm{CH}_{2}$ twist, and $\mathrm{C}-\mathrm{CH}_{3}$ stretching vibrations. Another positive-negative couplet in the $1200-1280-\mathrm{cm}^{-1}$ region originates from different $\mathrm{CH}_{2}$ twisting vibrations. The third positive-negative couplet in the $1300-1350-\mathrm{cm}^{-1}$ region originates from the $\mathrm{CH}_{2}$ wagging motions and a methine bending vibration coupled to $\mathrm{CH}_{2}$ wagging. The couplet associated with the 1423 - and $1459-\mathrm{cm}^{-1}$ Raman bands cannot be easily assigned to a specific pair of modes. The calculated frequencies indicate that there are several modes that contribute to the observed bands in this region.

The $1000-1500-\mathrm{cm}^{-1}$ region has several vibrational modes with significant overlap. Such crowding in the spectrum makes it difficult to draw useful correlations with the molecular structure because slight perturbations can lead to rearrangements in the order of the predicted bands and therefore uncertainties in interpretations. These uncertainties are probably responsible for the poor correlation between the predicted and observed ROA features in this region. One way to improve the situation here is to adjust the force constants by verifying and fitting the calculated vibrational frequencies and intensities to the corresponding experimental data for isotopic molecules, but the experimental data for isotopic molecules in this region are not available.

Couplet at $\sim 1700 \mathrm{~cm}^{-1}$. Only one $\mathrm{C}=\mathrm{O}$ stretching band is expected for methylcyclohexanone if this molecule has just one predominant conformer. The strong Raman band at $1710 \mathrm{~cm}^{-1}$ with a weak shoulder at $1713 \mathrm{~cm}^{-1}$ and the presence of a bisignate couplet (or possibly a triplet) associated with these bands suggest that either methylcyclohexanone exists as two or more different conformers or the weak band at $1713 \mathrm{~cm}^{-1}$ is due to one or more nonfundamental vibrations. Since the literature data point to the predominance of a single conformation, and the experimental Raman spectrum also has weak bands in the $1600-1680-\mathrm{cm}^{-1}$ region which cannot be associated with any fundamental modes, it is very likely that the weak Raman band at $1713 \mathrm{~cm}^{-1}$ and the associated weak ROA features are due to nonfundamental vibrations. The possibility for a ROA artifact here can be verified by measuring the ROA spectrum for the ( - )-enantiomer, but this enantiomer is currently not available. The possibility that the ROA structure in this region is associated with Fermi resonance involving the $\mathrm{C}=\mathrm{O}$ stretch and one or more overtones should also be considered since Escribano ${ }^{41}$ has shown theoretically that the interaction between a fundamental and an overtone can take the form of a characteristic bisignate couplet.
$\mathrm{CH}_{3}$ Group Bending Vibrations. In the early stages of the development of VOA, it was thought ${ }^{42.43}$ that the two asymmetric

[^4]bending motions of the methyl group might serve as chiral probes, since these two modes are expected to give a bisignate couplet that could reveal the absolute configuration at the chiral center. However, these two modes in most cases have nearly the same vibrational frequency, which is also the case here for methylcyclohexanone (Table I), resulting in mutual cancellation of their ROA. The symmetric bending vibration of the methyl group usually has weak Raman and ROA intensities in the depolarized spectra and in most cases is overlapped by the other $\mathrm{C}-\mathrm{H}$ bending vibrations. Noting that the methyl torsion vibration also has very weak Raman and ROA and the two methyl rocking modes have mutually cancelling unresolved ROA (vide supra), the methyl group vibrations are unlikely to be useful as probes of absolute configuration in the solution phase. This situation can be different if ROA studies are carried out on matrix isolated molecules, where closely spaced vibrations might be resolvable.

## Conclusions

The predicted Raman and ROA spectra are found to be in reasonable agreement with the experimental observations. In particular, the overall ROA sign pattern observed for ( + )-3methylcyclohexanone is well reproduced by the calculations for $(R)$-3-methylcyclohexanone. Since the $(+)$-enantiomer is indeed known to have the ( $R$ )-configuration, and the conformation used here is known to be the dominant conformer, this observation renders support for the $a b$ initio theoretical model employed and suggests that the absolute configurations can be predicted confidently with ROA. The vibrational assignments resulting from the current abinitio study point to the difficulties in placing reliance on those deduced from the empirical vibrational analysis. In a medium-size molecule such as methylcyclohexanone, the numerous vibrations that overlap in the limited vibrational
frequency region make it generally difficult to confidently hypothesize (on the basis of group assignments and intuition) the vibrational origin of the observed bands. It is therefore necessary to exercise caution in deducing the conformation or absolute configuration from the hypothesized vibrational assignments. In particular it is often tempting to associate a bisignate couplet with orthogonal modes such as in-phase and out-of-phase combinations of vibrational coordinates because such modes can be predicted with empirical models to have oppositely signed ROA. However, one should seriously consider the frequency separation between such modes, the possibility that one of the modes may not have significant intensity due to coupling with other internal coordinates, and that a different vibrational band can appear in the immediate vicinity. These factors are difficult to know beforehand, and interpretations of measured VOA spectra therefore demand reliable VOA calculations. The present $a b$ initio ROA calculation should not be taken as the final word, however, due to the uncertainties in the $a b$ initio force constants expected at the level of theory employed and also due to the uncertainties in correlating the predicted and observed bands when the bands are closely spaced. Nevertheless, the agreement between the experimental and predicted Raman spectra and between the experimental and predicted ROA sign patterns provides some confidence in the interpretations resulting from the present calculations.

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